



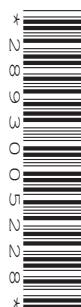
Cambridge International AS & A Level

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FURTHER MATHEMATICS

9231/13

Paper 1 Further Pure Mathematics 1

May/June 2024

2 hours

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has **20** pages. Any blank pages are indicated.



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$$\mathbf{A} = \begin{pmatrix} k & 1 & 0 \\ 6 & 5 & 2 \\ -1 & 3 & -k \end{pmatrix},$$

(a) Show that $\mathbf{A}$ is non-singular.

[2]

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(a) Find a cubic equation whose roots are $\alpha^2 + 1, \beta^2 + 1, \gamma^2 + 1$.

[3]



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3 The matrix $\mathbf{M}$ is given by $\mathbf{M} = \begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 7 & 0 \\ 0 & 1 \end{pmatrix}$.

(a) The matrix $\mathbf{M}$ represents a sequence of two geometrical transformations in the x - y plane.

Give full details of each transformation, and make clear the order in which they are applied. [4]

(b) Find the equations of the invariant lines, through the origin, of the transformation represented by $\mathbf{M}$. [5]





The triangle DEF in the x - y plane is transformed by $\mathbf{M}$ onto triangle PQR .

- (c) Given that the area of triangle PQR is 35 cm^2 , find the area of triangle DEF . [2]



$$\sum_{r=1}^n r^2 = \frac{1}{6}n(n+1)(2n+1).$$

[5]





5

show that $S_n = \frac{1}{30}n(n+1)(2n+1)(3n^2+3n-1)$. [6]

(c) Find the value of $\lim_{n \rightarrow \infty} (n^{-5} S_n)$. [2]

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1

Obtain an equation of Π_2 in the form $ax + by + cz = d$. [3]



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(a) Show that C has no vertical asymptotes and state the equation of the horizontal asymptote. [2]



- (b)** Find the coordinates of any stationary points on C . [4]



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- (c) Sketch C , stating the coordinates of the intersections with the axes.

[3]

- (d) Sketch $y^2 = \frac{x+1}{x^2+3}$, stating the coordinates of the stationary points and the intersections with the axes. [4]



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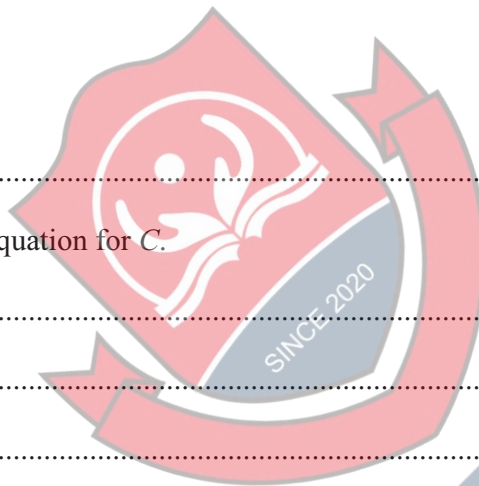
7 The curve C has polar equation $r^2 = \sin 2\theta \cos \theta$, for $0 \leq \theta \leq \pi$.

(a) Sketch C and state the equation of the line of symmetry.

[3]

(b) Find a Cartesian equation for C .

[3]



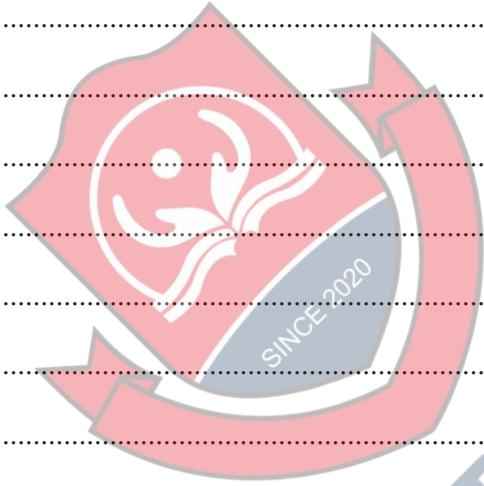
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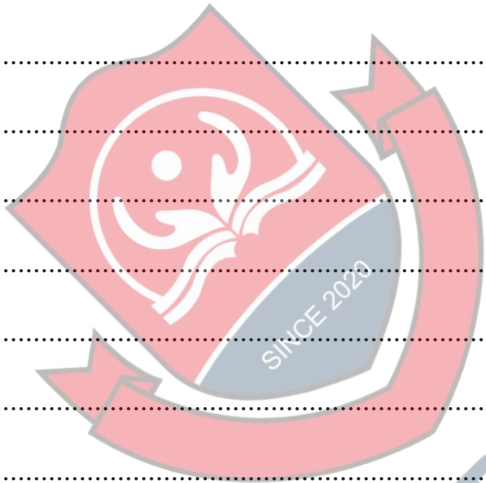




[4]

[6]





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