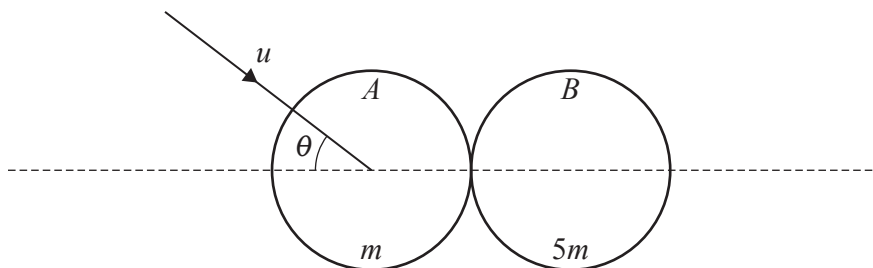


1

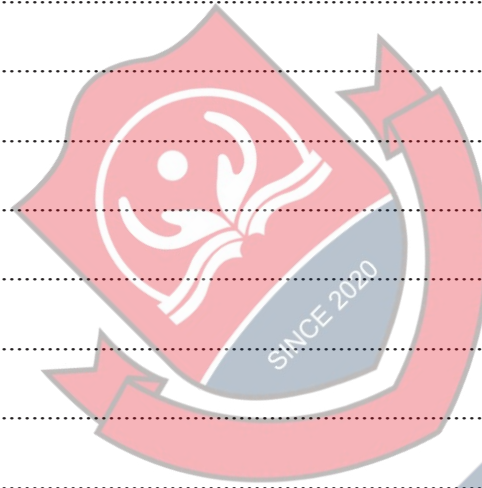


Two smooth uniform spheres A and B of equal radii have masses m and $5m$ respectively. Sphere A is moving on a smooth horizontal surface with speed u when it collides with sphere B which is at rest on the surface. Immediately before the collision, A 's direction of motion makes an angle of θ with the line of centres. After the collision, the kinetic energies of A and B are equal. The coefficient of restitution between the spheres is $\frac{1}{2}$.

Find the value of $\tan \theta$.

[6]



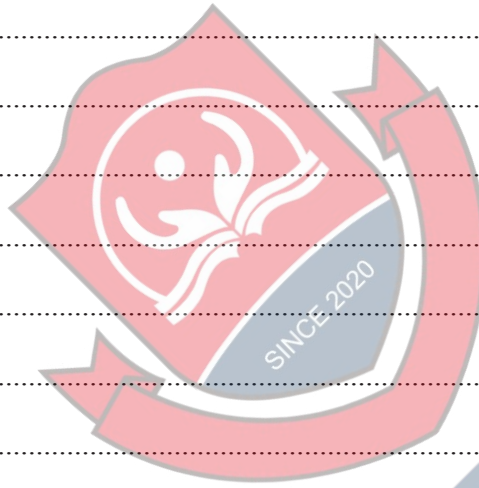


4Uadmission

- 2 The points A and B are at the same horizontal level a distance $4a$ apart. The ends of a light elastic string, of natural length $4a$ and modulus of elasticity λ , are attached to A and B . A particle P of mass m is attached to the midpoint of the string. The system is in equilibrium with P at a distance $\frac{3}{2}a$ below M , the midpoint of AB .

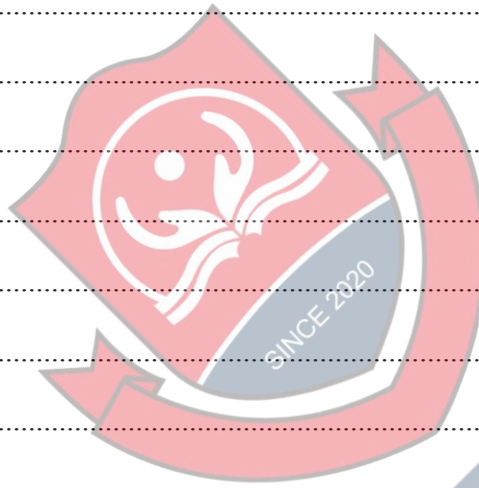
(a) Find λ in terms of m and g .

[3]



The particle P is pulled down vertically and released from rest at a distance $\frac{8}{3}a$ below M .

- (b) Find, in terms of a and g , the speed of P as it passes through M in the subsequent motion. [4]

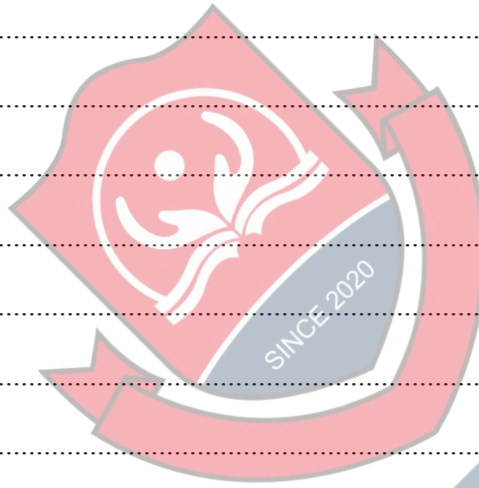


- 3 At time $t = 0$ seconds, a particle P is projected with speed $u \text{ m s}^{-1}$ at an angle 60° above the horizontal from a point O . In the subsequent motion P moves freely under gravity. The direction of motion of P when $t = 5$ is perpendicular to its direction of motion when $t = 15$.

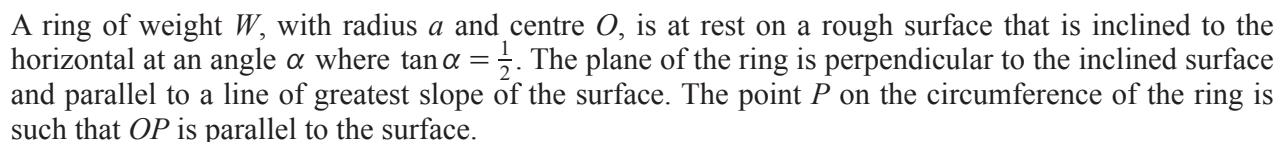
Find the value of u .

[5]





4Uadmission



A light inextensible string is attached to P and to the point Q , which is on the surface, such that PQ is horizontal (see diagram). The points O, P and Q are in the same vertical plane. The system is in limiting equilibrium and the coefficient of friction between the ring and the surface is μ .

- (a) Find, in terms of W , the tension in the string PQ . [4]

(b) Find the value of μ .

[3]



- 5 Two particles A and B of masses m and km respectively are connected by a light inextensible string of length a . The particles are placed on a rough horizontal circular turntable with the string taut and lying along a radius of the turntable. Particle A is at a distance a from the centre of the turntable and particle B is at a distance $2a$ from the centre of the turntable. The coefficient of friction between each particle and the turntable is $\frac{1}{5}$.

When the turntable is made to rotate with angular speed $\frac{2}{5}\sqrt{\frac{g}{a}}$, the system is in limiting equilibrium.

- (a) Find the tension in the string, in terms of m and g . [4]



(b) Find the value of k .

[3]



- $\frac{1}{10}(2v-1)^2 e^{-t}$ N and acts towards O . When $t = 0$, $x = 1$ and $v = 3$.

[5]

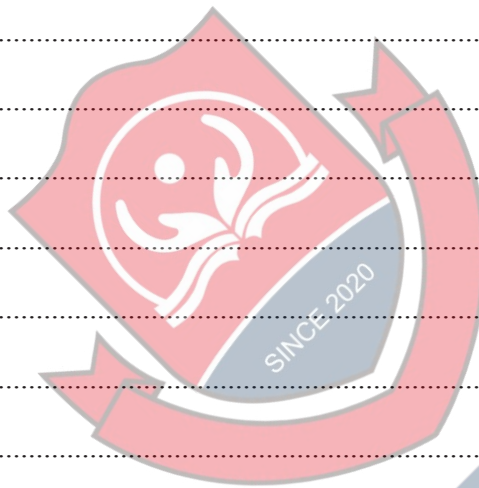
(b) Find an expression for x in terms of t .

[4]

The image features the University of Alberta logo in the top left corner, which includes a stylized red and white flower and the text 'SINCE 2020'. A large, light blue diagonal watermark reading '4U Admission' is overlaid across the entire page. The background is white with horizontal dotted lines.

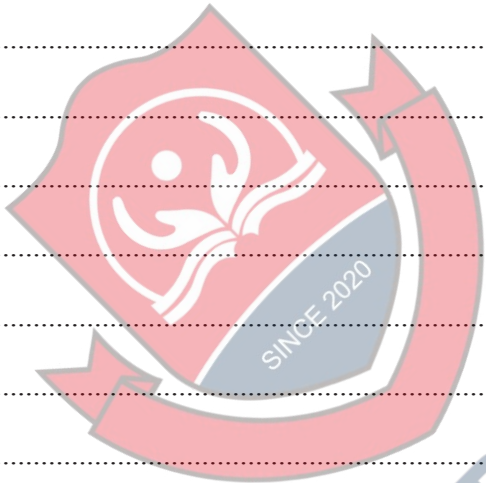
- 7 A smooth sphere with centre O and of radius a is fixed to a horizontal plane. A particle P of mass m is projected horizontally from the highest point of the sphere with speed u , so that it begins to move along the surface of the sphere. The particle P loses contact with the sphere at the point Q on the sphere, where OQ makes an angle θ with the upward vertical through O .

(a) Show that $\cos \theta = \frac{u^2 + 2ag}{3ag}$. [4]



It is given that $\cos \theta = \frac{5}{6}$.

- (b)** Find, in terms of a and g , an expression for the vertical component of the velocity of P just before it hits the horizontal plane to which the sphere is fixed. [3]

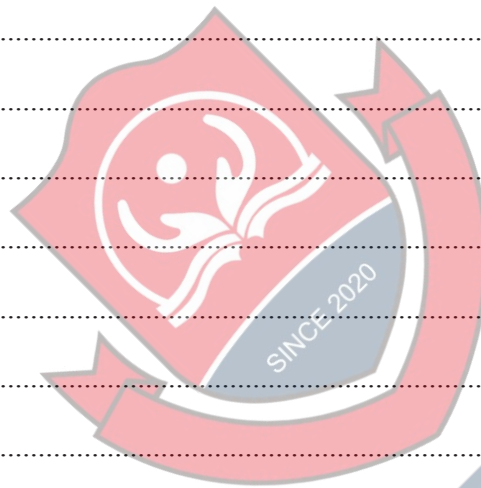


- (c) Find an expression for the time taken by P to fall from Q to the plane. Give your answer in the form $k\sqrt{\frac{a}{g}}$, stating the value of k correct to 3 significant figures. [2]



Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.



4Uadmission

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of Cambridge Assessment. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which is a department of the University of Cambridge.