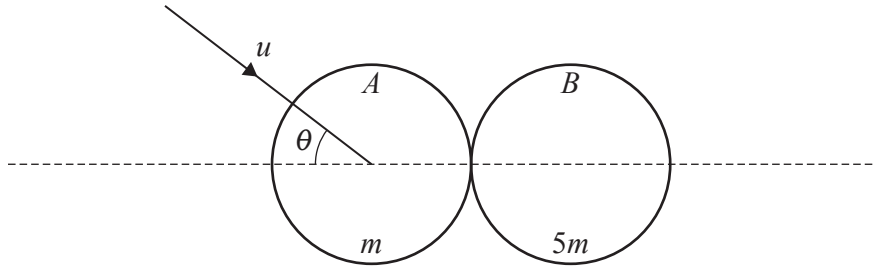


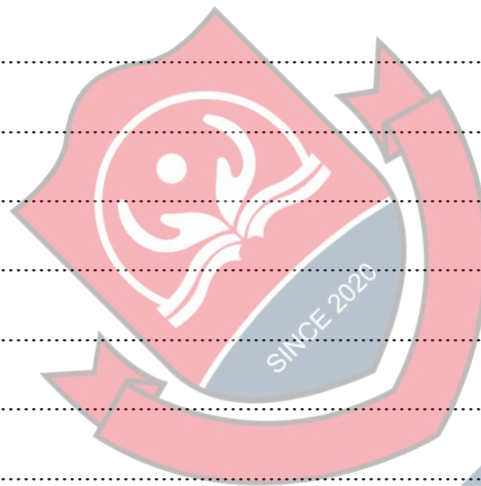
1



Two smooth uniform spheres A and B of equal radii have masses m and $5m$ respectively. Sphere A is moving on a smooth horizontal surface with speed u when it collides with sphere B which is at rest on the surface. Immediately before the collision, A 's direction of motion makes an angle of θ with the line of centres. After the collision, the kinetic energies of A and B are equal. The coefficient of restitution between the spheres is $\frac{1}{2}$.

Find the value of $\tan \theta$.

[6]



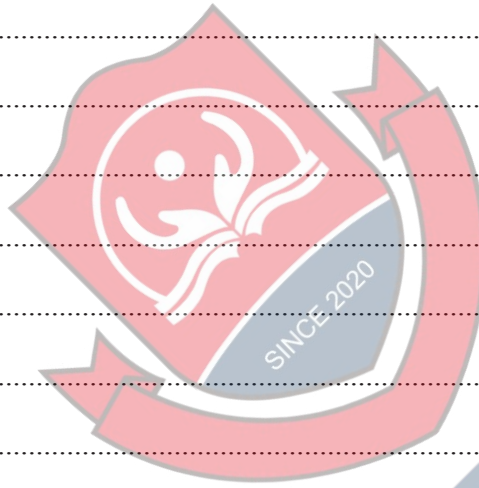


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- 2 The points A and B are at the same horizontal level a distance $4a$ apart. The ends of a light elastic string, of natural length $4a$ and modulus of elasticity λ , are attached to A and B . A particle P of mass m is attached to the midpoint of the string. The system is in equilibrium with P at a distance $\frac{3}{2}a$ below M , the midpoint of AB .

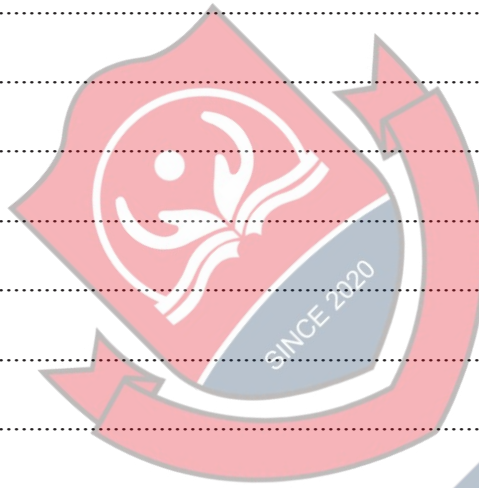
(a) Find λ in terms of m and g .

[3]



The particle P is pulled down vertically and released from rest at a distance $\frac{8}{3}a$ below M .

- (b) Find, in terms of a and g , the speed of P as it passes through M in the subsequent motion. [4]

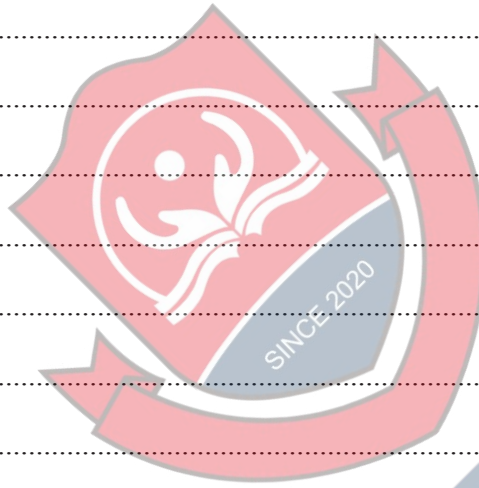


- 3 At time $t = 0$ seconds, a particle P is projected with speed $u \text{ m s}^{-1}$ at an angle 60° above the horizontal from a point O . In the subsequent motion P moves freely under gravity. The direction of motion of P when $t = 5$ is perpendicular to its direction of motion when $t = 15$.

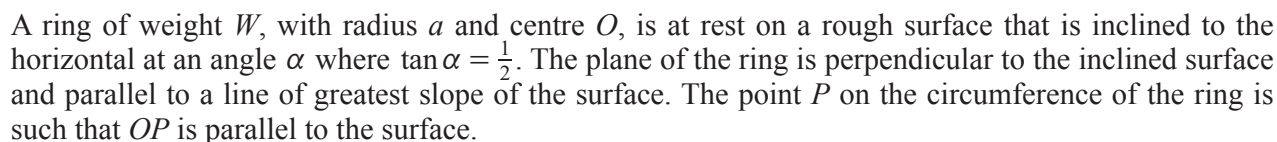
Find the value of u .

[5]





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A light inextensible string is attached to P and to the point Q , which is on the surface, such that PQ is horizontal (see diagram). The points O, P and Q are in the same vertical plane. The system is in limiting equilibrium and the coefficient of friction between the ring and the surface is μ .

- (a) Find, in terms of W , the tension in the string PQ . [4]



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(b) Find the value of μ .

[3]



- 5 Two particles A and B of masses m and km respectively are connected by a light inextensible string of length a . The particles are placed on a rough horizontal circular turntable with the string taut and lying along a radius of the turntable. Particle A is at a distance a from the centre of the turntable and particle B is at a distance $2a$ from the centre of the turntable. The coefficient of friction between each particle and the turntable is $\frac{1}{5}$.

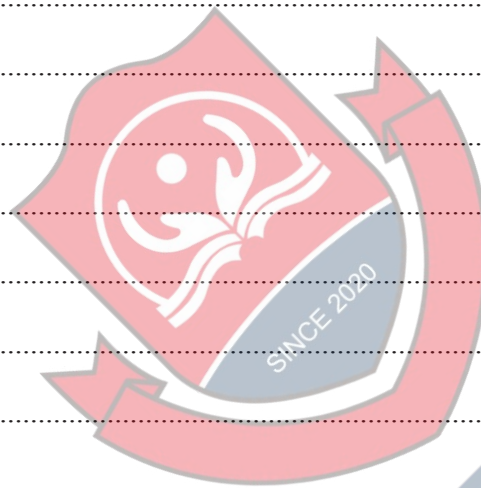
When the turntable is made to rotate with angular speed $\frac{2}{5}\sqrt{\frac{g}{a}}$, the system is in limiting equilibrium.

- (a) Find the tension in the string, in terms of m and g . [4]



(b) Find the value of k .

[3]



- A particle P of mass 2 kg moving on a horizontal straight line has displacement $x\text{ m}$ from a fixed point O on the line and velocity $v\text{ m s}^{-1}$ at time $t\text{ s}$. The only horizontal force acting on P has magnitude $\frac{1}{10}(2v-1)^2\text{ e}^{-t}\text{ N}$ and acts towards O . When $t = 0$, $x = 1$ and $v = 3$.

(a) Find an expression for v in terms of t .

[5]

The image features the University of Alberta logo in the top left corner, which includes a stylized red and white flower and a blue shield with the text 'SINCE 2020'. A large, light blue, diagonal watermark reading '4U Admission' is overlaid across the entire page. The background is white with horizontal dotted lines.

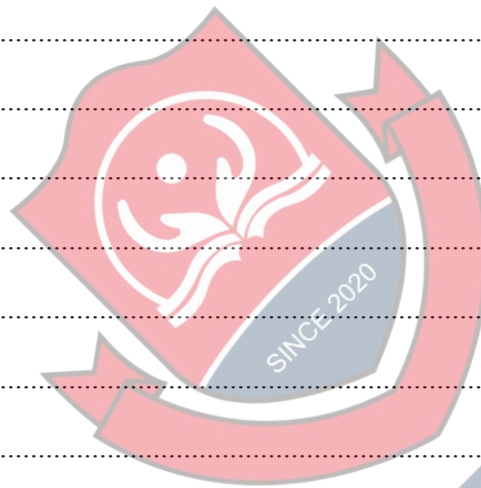
(b) Find an expression for x in terms of t .

[4]

The image features the University of Alberta logo in the top left corner, which includes a stylized red and white flower and the text 'SINCE 2020'. A large, diagonal, light blue watermark reading '4U Admission' is overlaid across the entire page. The background is white with horizontal dotted lines.

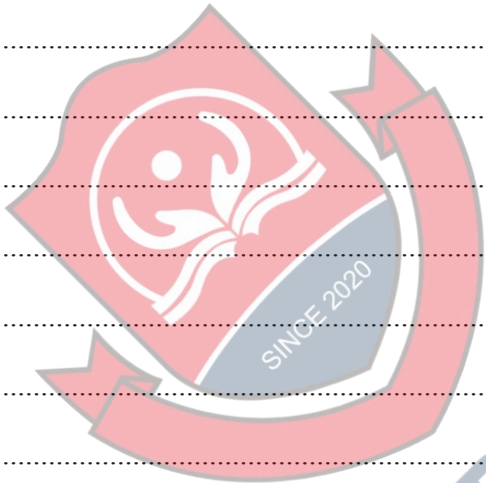
- 7 A smooth sphere with centre O and of radius a is fixed to a horizontal plane. A particle P of mass m is projected horizontally from the highest point of the sphere with speed u , so that it begins to move along the surface of the sphere. The particle P loses contact with the sphere at the point Q on the sphere, where OQ makes an angle θ with the upward vertical through O .

(a) Show that $\cos \theta = \frac{u^2 + 2ag}{3ag}$. [4]



It is given that $\cos \theta = \frac{5}{6}$.

- (b)** Find, in terms of a and g , an expression for the vertical component of the velocity of P just before it hits the horizontal plane to which the sphere is fixed. [3]

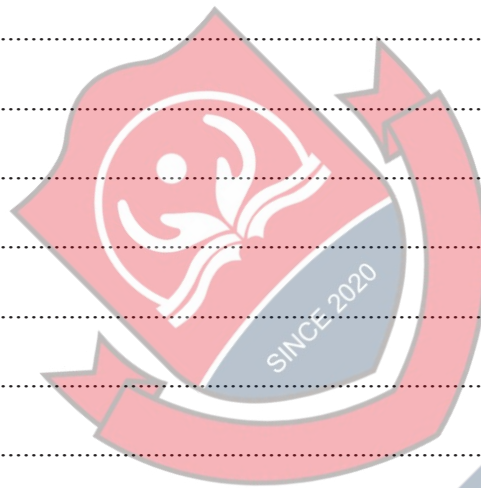


- (c) Find an expression for the time taken by P to fall from Q to the plane. Give your answer in the form $k\sqrt{\frac{a}{g}}$, stating the value of k correct to 3 significant figures. [2]



Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.



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