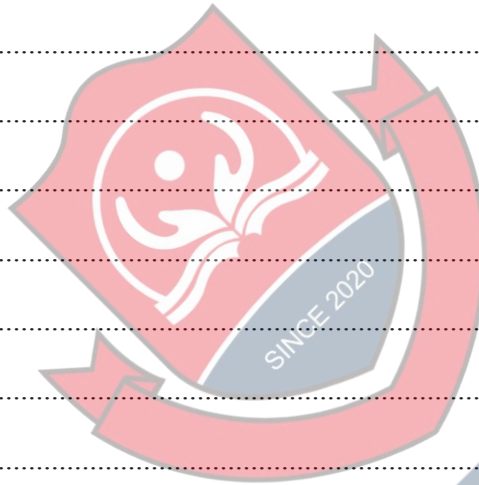


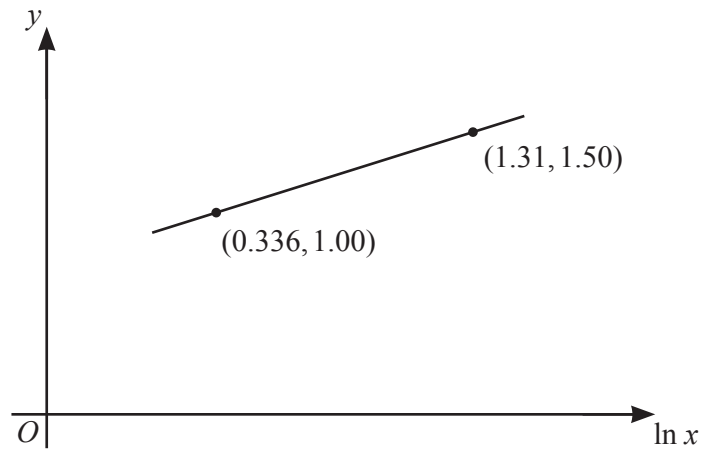
- 1 Expand $(3+x)(1-2x)^{\frac{1}{2}}$ in ascending powers of x , up to and including the term in x^2 , simplifying the coefficients. [4]



- 2 Solve the equation $\ln(x-5) = 7 - \ln x$. Give your answer correct to 2 decimal places. [4]



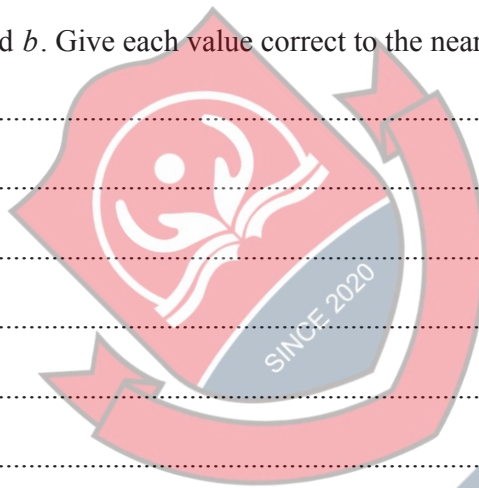
3



The variables x and y satisfy the equation $a^y = bx$, where a and b are constants. The graph of y against $\ln x$ is a straight line passing through the points $(0.336, 1.00)$ and $(1.31, 1.50)$, as shown in the diagram.

Find the values of a and b . Give each value correct to the nearest integer.

[4]



4 The complex number u is given by $u = -1 - i\sqrt{3}$.

- (a) Express u in the form $r(\cos \theta + i \sin \theta)$, where $r > 0$ and $-\pi < \theta \leq \pi$. Give the exact values of r and θ . [2]



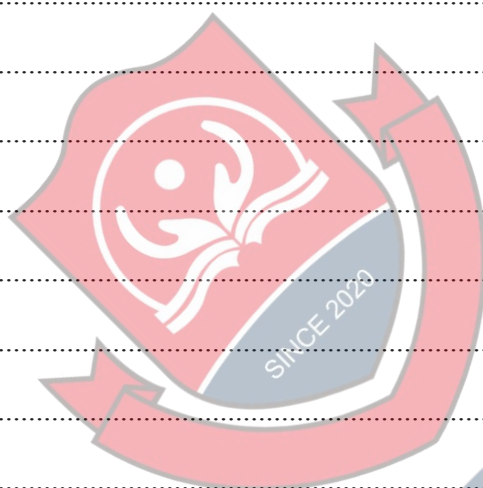
The complex number v is given by $v = 5\left(\cos \frac{1}{6}\pi + i \sin \frac{1}{6}\pi\right)$.

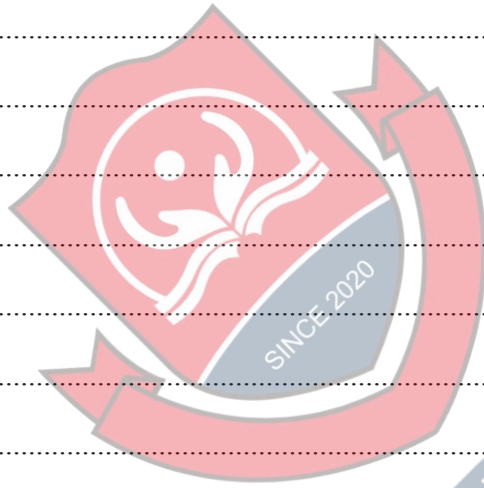
- (b)** Express the complex number $\frac{v}{u}$ in the form $re^{i\theta}$ where $r > 0$ and $-\pi < \theta \leq \pi$. [2]

4Uadn

- 5** The equation of a curve is $y = \frac{e^{\sin x}}{\cos^2 x}$ for $0 \leq x \leq 2\pi$.

Find $\frac{dy}{dx}$ and hence find the x -coordinates of the stationary points of the curve. [7]

The image shows a white background with horizontal dotted lines. In the top left corner is a partial view of the University of the Pacific logo, which includes a red shield with a white cross and the text 'SINCE 2020'. A large, light blue diagonal watermark with the text '4Uadmission' is overlaid across the entire page.



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- 6 (a)** By sketching a suitable pair of graphs, show that the equation $\operatorname{cosec} \frac{1}{2}x = e^x - 3$ has exactly one root, denoted by α , in the interval $0 < x < \pi$. [2]

(b) Verify by calculation that α lies between 1 and 2.

[2]

- (c) Show that if a sequence of values in the interval $0 < x < \pi$ given by the iterative formula

$$x_{n+1} = \ln(\operatorname{cosec} \frac{1}{2}x_n + 3)$$

converges, then it converges to α .

[1]

[illegible]

- (d) Use this iterative formula with an initial value of 1.4 to determine α correct to 2 decimal places. Give the result of each iteration to 4 decimal places. [3]



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- (e) State the minimum number of calculated iterations needed with this initial value to determine α correct to 2 decimal places. [1]

.....



- [4]

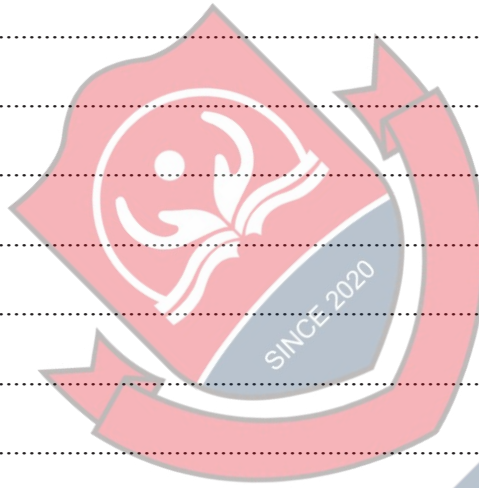
[2]

- 8** Use the substitution $u = 1 - \sin x$ to find the exact value of

$$\int_{\pi}^{\frac{3}{2}\pi} \frac{\sin 2x}{\sqrt{1 - \sin x}} dx.$$

Give your answer in the form $a+b\sqrt{2}$ where a and b are rational numbers to be determined. [7]





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- 9** The equations of two straight lines l_1 and l_2 are

$$l_1: \quad \mathbf{r} = \mathbf{i} - 2\mathbf{j} + 3\mathbf{k} + \lambda(2\mathbf{i} - \mathbf{j} + a\mathbf{k}) \quad \text{and} \quad l_2: \quad \mathbf{r} = -\mathbf{i} - \mathbf{j} - \mathbf{k} + \mu(3\mathbf{i} - 2\mathbf{j} - 2\mathbf{k}),$$

where a is a constant.

The lines l_1 and l_2 are perpendicular.

- (a)** Show that $a = 4$. [1]

The lines l_1 and l_2 also intersect.

- (b)** Find the position vector of the point of intersection. [4]

40

The point A has position vector $-5\mathbf{i} + \mathbf{j} - 9\mathbf{k}$.

- (c) Show that A lies on l_1 . [2]



The point B is the image of A after a reflection in the line l_2 .

- (d) Find the position vector of B . [2]

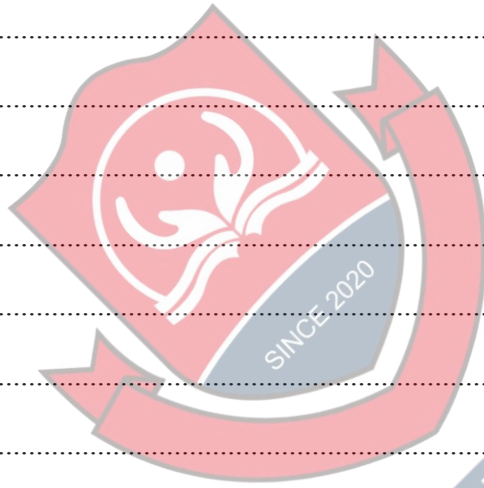
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- 10 (a)** Given that $2x = \tan y$, show that $\frac{dy}{dx} = \frac{2}{1+4x^2}$. [3]



- (b) Hence find the exact value of $\int_{\frac{1}{2}}^{\frac{\sqrt{3}}{2}} x \tan^{-1}(2x) dx$. [7]

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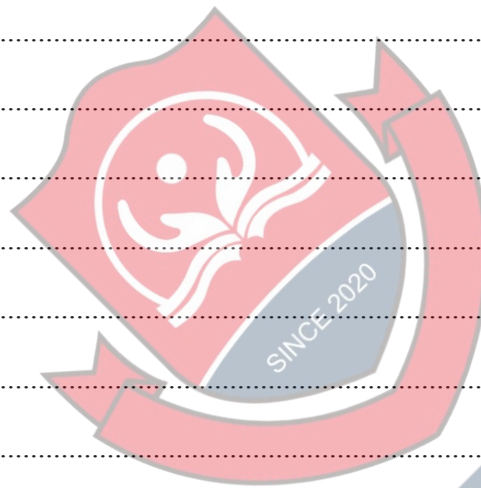
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- (a)** Show that x and t satisfy the differential equation

$$1495 \frac{dx}{dt} = x(300 - x). \quad [2]$$

- (b) Using partial fractions, solve the differential equation and obtain an expression for t in terms of a single logarithm involving x . [9]

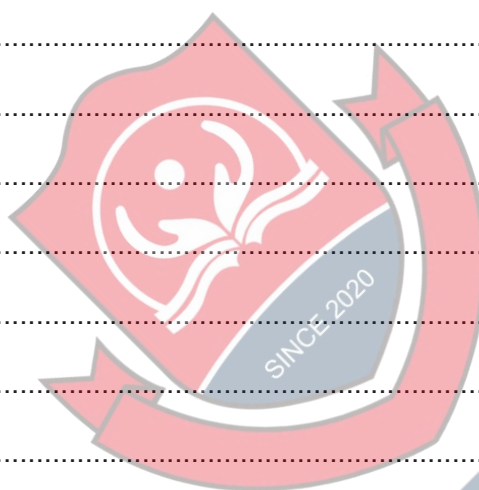
differential equation and obtain an expression for t



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Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.



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