



Cambridge International AS & A Level

CANDIDATE
NAME
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MATHEMATICS

9709/12

Paper 1 Pure Mathematics 1

October/November 2024

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

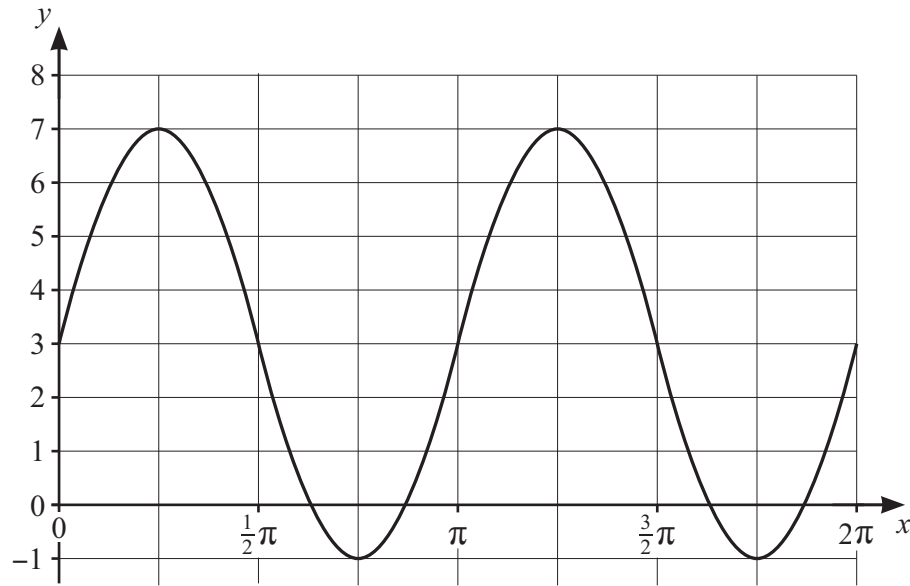
INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has **20** pages. Any blank pages are indicated.



1



The diagram shows the curve with equation $y = a \sin(bx) + c$ for $0 \leq x \leq 2\pi$, where a , b and c are positive constants.

- (a) State the values of a , b and c . [3]

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- (b) For these values of a , b and c , determine the number of solutions in the interval $0 \leq x \leq 2\pi$ for each of the following equations:

(i) $a \sin(bx) + c = 7 - x$ [1]

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(ii) $a \sin(bx) + c = 2\pi(x - 1)$. [1]

.....

.....



(a) Find the sum of the first 20 terms of the progression.

[2]

[illegible]

(b) Find the value of k .

[3]



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(a) $\left(x + \frac{3}{x^2}\right)^6$

[illegible]

(b) $(4x^3 - 5)\left(x + \frac{3}{x^2}\right)^6$.

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5 The function f is defined by $f(x) = \frac{2x+1}{2x-1}$ for $x < \frac{1}{2}$.

(a) (i) State the value of $f(-1)$.

[1]

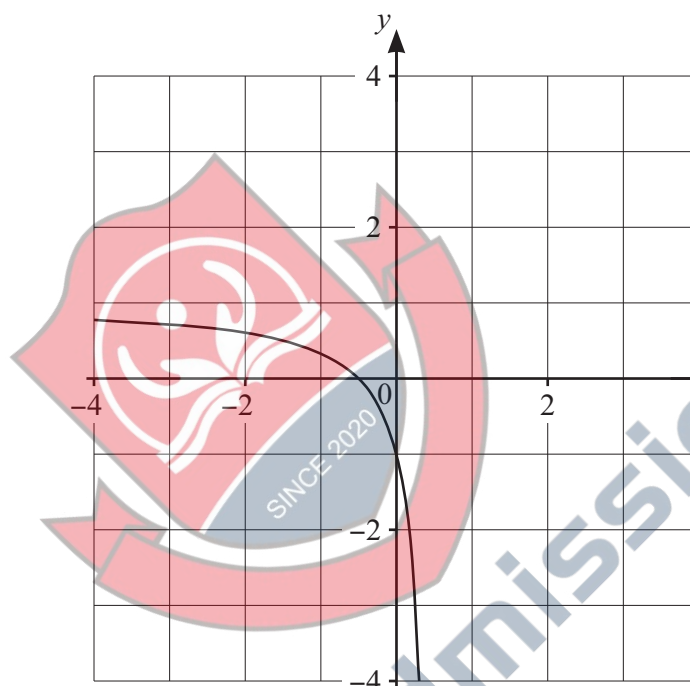
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(ii)



The diagram shows the graph of $y = f(x)$. Sketch the graph of $y = f^{-1}(x)$ on this diagram. Show any relevant mirror line.

[2]

(iii) Find an expression for $f^{-1}(x)$ and state the domain of the function f^{-1} .

[4]

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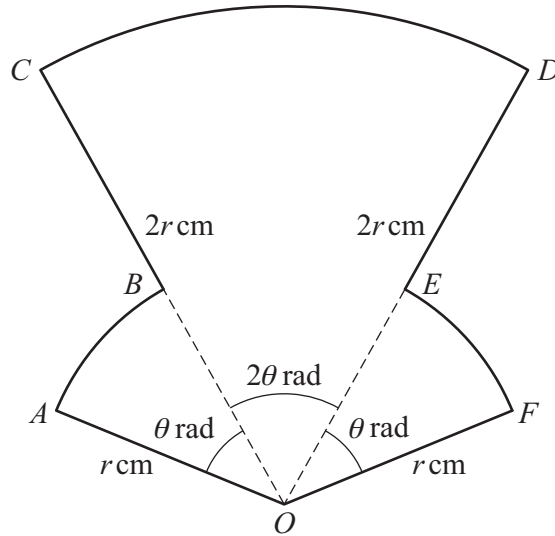
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(b) Solve the equation $f(x) = gf\left(\frac{1}{4}\right)$.

[3]



The diagram shows a metal plate $OABCDEF$ consisting of sectors of two circles, each with centre O . The radii of sectors AOB and EOF are r cm and the radius of sector COD is $2r$ cm. Angle $AOB = \text{angle } EOF = \theta$ radians and angle $COD = 2\theta$ radians.

It is given that the perimeter of the plate is 14 cm and the area of the plate is 10 cm^2 .

Given that $r > \frac{3}{2}$ and $\theta < \frac{3}{4}$, find the values of r and θ .

[6]



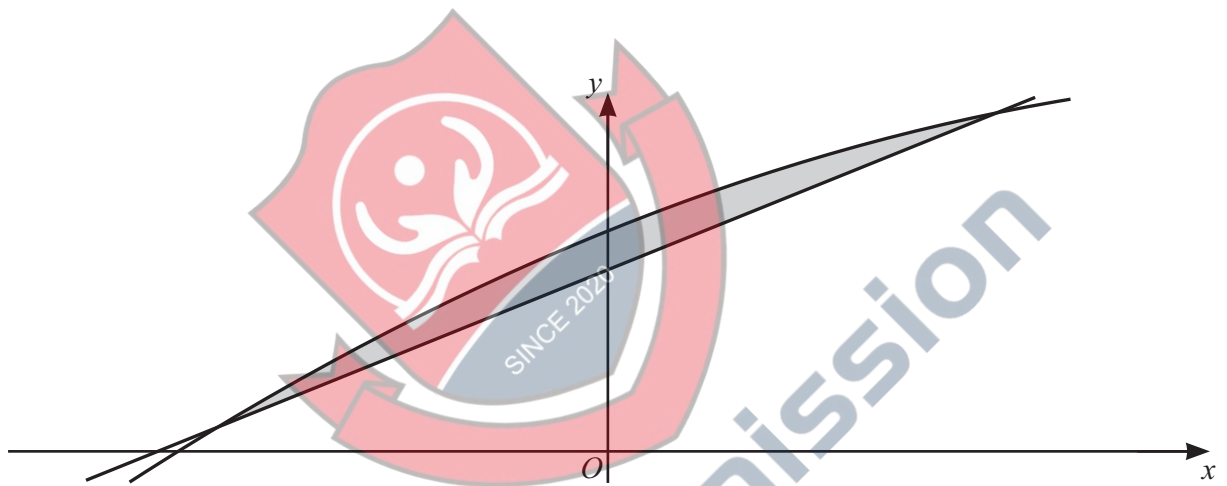




- 7 (a) By expressing $-2x^2 + 8x + 11$ in the form $-a(x-b)^2 + c$, where a , b and c are positive integers, find the coordinates of the vertex of the graph with equation $y = -2x^2 + 8x + 11$. [3]

[illegible]

(b)



The diagram shows part of the curve with equation $y = -2x^2 + 8x + 11$ and the line with equation $y = 8x + 9$.

Find the area of the shaded region.





- [illegible]

(b) (i) Find the equation of the normal to the circle at the point A . [3]



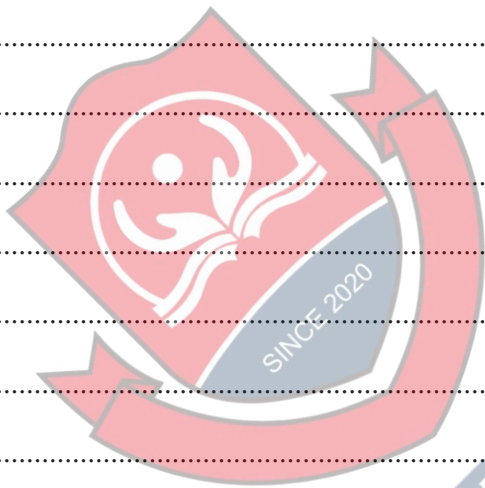
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[5]



- Find the values of k and p , and find the coordinates of the other point of intersection. [7]

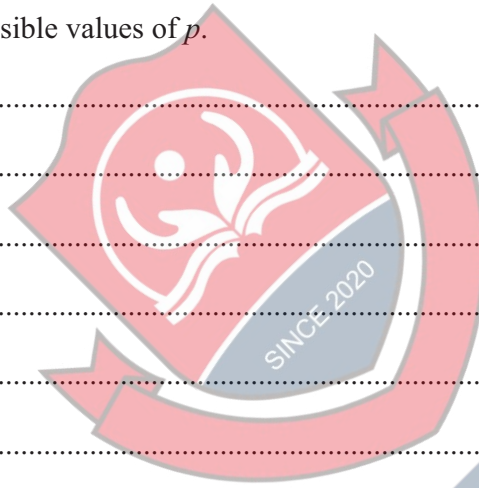


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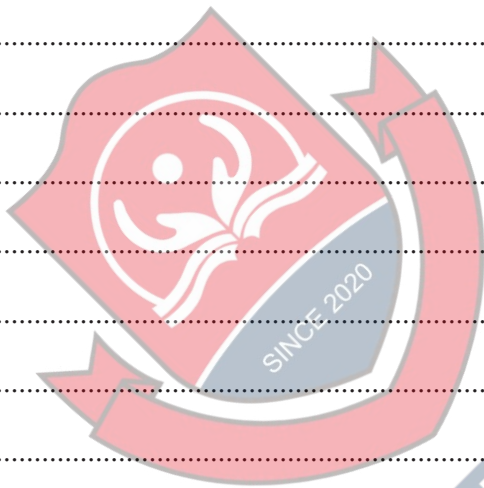
Find the set of possible values of p .

[3]

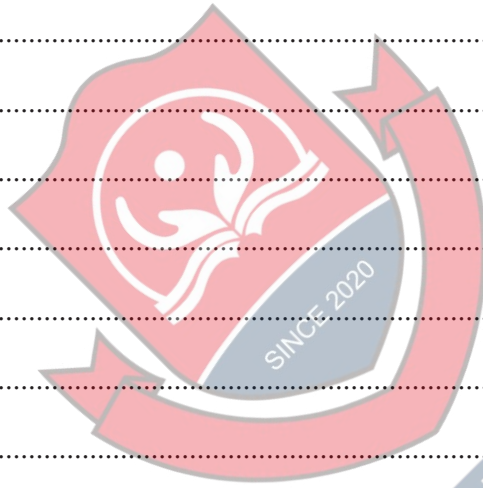




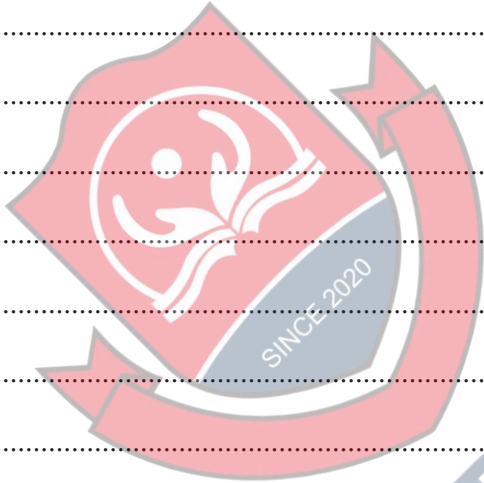
(c) Determine, making your reasoning clear, whether f is an increasing function, a decreasing function or neither. [3]



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If you use the following page to complete the answer to any question, the question number must be clearly shown.



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